

PROBLEMS AND SOLUTIONS - SOLVING TRIGONOMETRIC EQUATIONS - PART 2 Prepared by Ingrid Stewart, Ph.D., College of Southern Nevada Please Send Questions and Comments to ingrid.stewart@csn.edu. Thank you!

PLEASE NOTE THAT YOU CANNOT ALWAYS USE A CALCULATOR ON THE ACCUPLACER - COLLEGE-LEVEL MATHEMATICS TEST! YOU MUST BE ABLE TO DO SOME PROBLEMS WITHOUT A CALCULATOR!

Problem 1:

Solve **2 cos** $x = -\sqrt{3}$ for x finding **ALL** possible solutions. Express your answer in **EXACT** radians AND in **EXACT** degrees.

Problem 2:

Solve tan x = -12.08 for x finding ALL possible solutions. Express your answers in degrees.

Problem 3:

Solve $2 \sin^2 x = 3 \sin x - 1$ for x on the interval $[0^\circ, 360^\circ]$. Express your answers in degrees.

Problem 4:

Solve $2\cos^2 x + 3\sin x = 0$ for x on the interval $[0^\circ, 360^\circ]$. Express your answers in degrees.

Problem 5:

Solve $2\cos x + 2\sin x \cos x = 0$ for x finding ALL solutions. Express your answers in **EXACT** radians.

Problem 6:

Solve $\tan^2 x = 3$ for x on the interval $(0,2\pi)$. Express your answers in **EXACT** radians.

Problem 7:

Solve $1-\sqrt{2}\cos(\frac{x}{2})=0$ for x on the interval $[0^{\circ},720^{\circ}]$. Express your answers in degrees.

Problem 8:

Solve $2\cos 2x = -1$ for x on the interval $[0^{\circ},180^{\circ}]$. Express your answers in degrees.

Problem 9:

Solve $2 \sin 4x = 1$ for x on the interval $[0, \pi]$. Express your answers in radians.

Problem 10:

Solve $2 \tan \frac{x}{3} = -2$ for x on the interval $[0,6\pi]$. Express your answers in radians.

Problem 11:

Solve $\sin 3x = -1$ for x on the interval $\left[0, \frac{2\pi}{3}\right]$. Express your answers in radians.

Problem 12:

Solve $\cos 4x = 0$ for x on the interval $\left[0, \frac{\pi}{2}\right]$. Express your answers in radians.

SOLUTIONS

You can find detailed solutions below the link for this problem set!

1.	2.	3.
$\frac{5\pi}{6} + 2\pi k$, $\frac{7\pi}{6} + 2\pi k$	94 .73° + 360° k, 274 .73° + 360° k	$x_1 = 30^\circ$
150° + 360°k , 210° + 360°k	or 94 .73° + 180° k	$x_2 = 90^{\circ}$
where \boldsymbol{k} is any integer	where \boldsymbol{k} is any integer	$x_3 = 150^{\circ}$
4.	5.	6.
$x_1 = 210^{\circ}$	$\frac{\pi}{2} + 2\pi k$ and $\frac{3\pi}{2} + 2\pi k$	$x_i = 60^\circ \equiv \frac{\pi}{3}$
$x_2 = 330^{\circ}$	where k is any integer	$egin{aligned} oldsymbol{x}_{i} &= oldsymbol{60^{\circ}} \equiv rac{\pi}{3} \ oldsymbol{x}_{2} &= oldsymbol{240^{\circ}} \equiv rac{oldsymbol{4\pi}}{3} \end{aligned}$
		$x_3 = 120^\circ \equiv \frac{2\pi}{3}$
		$x_3 = 120^\circ \equiv \frac{2\pi}{3}$ $x_4 = 300^\circ \equiv \frac{5\pi}{3}$
		9.
7.	8.	$\boldsymbol{x}_{t} = \frac{\pi}{24}$
x, = 90°	x, = 60°	$x_1 = \frac{\pi}{24}$ $x_2 = \frac{5\pi}{24}$
$x_2 = 630^\circ$	x ₂ = 120°	
		$x_3 = \frac{13\pi}{24}$ $x_4 = \frac{17\pi}{24}$
		$X_4 = \frac{77\pi}{24}$
10.	11.	12.
$\boldsymbol{x}_{t} = \frac{\boldsymbol{9}\pi}{\boldsymbol{4}}$ $\boldsymbol{x}_{2} = \frac{\boldsymbol{2}\boldsymbol{1}\pi}{\boldsymbol{4}}$	$x = \frac{\pi}{2}$	$x_1 = \frac{\pi}{8}$ $x_2 = \frac{3\pi}{8}$
$\boldsymbol{x}_{2} = \frac{21\pi}{4}$		$x_2 = \frac{3\pi}{8}$