

PROBLEMS AND SOLUTIONS - SOLVING LOGARITHMIC EQUATIONS Prepared by Ingrid Stewart, Ph.D., College of Southern Nevada Please Send Questions and Comments to ingrid.stewart@csn.edu. Thank you!

PLEASE NOTE THAT YOU CANNOT ALWAYS USE A CALCULATOR ON THE ACCUPLACER - COLLEGE-LEVEL MATHEMATICS TEST! YOU MUST BE ABLE TO DO SOME PROBLEMS WITHOUT A CALCULATOR!

Problem 1:

Solve $\log_{a}(x+3)=2$. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x!

Problem 2:

Solve $\log(x-1) - \log(x+1) = 1$. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x!

Problem 3:

Solve $\ln x + \ln(2x - 1) = 2$. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x! Round to 4 decimal places.

Problem 4:

Solve $\log(4x + 2x^2) = \log(3x^2)$. Only find solutions that produce REAL numbers, except $\mathbf{0}$, in the original equation when substituting for \mathbf{x} !

This logarithmic equation contains only logarithmic expressions. Therefore, we can discard the word *log* on either side, leaving us with an algebraic equation

Problem 5:

Solve log(2x-1) = log(4x+3) - log x. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x!

Problem 6:

Solve $\log(x+4) - \log x = \log(x+2)$. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x! Round to 4 decimal places.

Problem 7:

Solve for x: $2 \ln x = \ln(2 - x) + \ln(4 - x)$. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x!

Problem 8:

Solve $\log(x-3) = \log(-x)$. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x!

Problem 9:

Solve $\log(3-\frac{1}{2}x) = \log(-x)$. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x!

Problem 10:

Solve $\log x^2 = \log(-5x - 6)$. Only find solutions that produce REAL numbers, except $\mathbf{0}$, in the original equation when substituting for \mathbf{x} !

Problem 11:

Solve $2 \log x = \log(-5x - 6)$. Only find solutions that produce REAL numbers, except 0, in the original equation when substituting for x!

Problem 12:

A medical technologist creates a reagent with a pH of 7.48. Find the concentration of hydrogen ions $[H^+]$ in the reagent using the formula $pH = -log[H^+]$. Express your answer in *Scientific Notation* rounded to two decimal places.

SOLUTIONS You can find detailed solutions below the link for this problem set!

1. 13	2. No solutions	3. 2.1883
4. 4	5. 3	6. 1.5616
7. 4/3	8. No solutions	9. -6
10. <i>-3, -2</i>	11. No solutions	12. 3.31 × 10 -8