

#### PROBLEMS AND SOLUTIONS

# ALGEBRAIC REPRESENTATIONS OF LINEAR EQUATIONS IN TWO VARIABLES Prepared by Ingrid Stewart, Ph.D., College of Southern Nevada Please Send Questions and Comments to ingrid.stewart@csn.edu. Thank you!

PLEASE NOTE THAT YOU CANNOT USE A CALCULATOR ON THE ACCUPLACER - ELEMENTARY ALGEBRA TEST! YOU MUST BE ABLE TO DO THE FOLLOWING PROBLEMS WITHOUT A CALCULATOR!

#### Problem 1:

Change the *slope-intercept form* of the linear equation  $\mathbf{y} = -\frac{4}{3} \mathbf{x} + \frac{8}{3}$  to *general form*  $\mathbf{A}\mathbf{x} + \mathbf{B}\mathbf{y} = \mathbf{C}$  so that the coefficient for  $\mathbf{x}$  and  $\mathbf{y}$  are integers with the coefficient for  $\mathbf{x}$  a positive integer.

#### **Problem 2:**

Change the *slope-intercept form* of the linear equation  $\mathbf{y} = \frac{1}{2} \mathbf{x} - \frac{7}{2}$  to *general form*  $\mathbf{A}\mathbf{x} + \mathbf{B}\mathbf{y} = \mathbf{C}$  so that the coefficient for  $\mathbf{x}$  and  $\mathbf{y}$  are integers with the coefficient for  $\mathbf{x}$  a positive integer.

## **Problem 3:**

Find the slope and the coordinates of the y-intercept, if they exist, for the lines described as follows:

a. 
$$y = -x + 3$$

b. 
$$y = \frac{4}{5}x - 1$$

c. 
$$y = 2x$$

f. 
$$y + 9 = 0$$

h. 
$$x + 24 = 0$$

#### **Problem 4:**

Find the slope and the coordinates of the y-intercept for the line 3x - y = -1.

## **Problem 5:**

Change the linear equation 2x - 3y = 6 to slope-intercept form y = mx + b.

#### **Problem 6:**

Change the linear equation  $3x + \frac{1}{4}y = 5$  to slope-intercept form y = mx + b.

### **Problem 7:**

Change the linear equation -7.8x + 3.9y - 11.7 = 0 to slope-intercept form y = mx + b

#### **Problem 8:**

Write the equation of the line with the given slope and y-intercept. For this we will use the slope-intercept form  $\mathbf{y} = \mathbf{m}\mathbf{x} + \mathbf{b}$ .

a. 
$$m = 2$$
,  $b = -5$ 

b. 
$$m = -5$$
,  $b = 0$ 

c. 
$$m = 3$$
,  $b = 1$ 

d. 
$$m = 0$$
,  $b = -7$ 

## **Problem 9:**

Find the equation of a line passing through the points (1, 2) and (3, 0). Solve the equation for y, if possible.

#### **Problem 10:**

Find the equation of a line passing through the points (1, 2) and (1, -5). Solve the equation for y, if possible.

#### Problem 11:

Find the equation of a line passing through the points (2, 1) and (-5, 1). Solve the equation for y, if possible.

## **Problem 12:**

Find the equation of a line given the point (-3,-1) and the slope  $m=-\frac{2}{3}$ . Express the equation in *general form*.

## **Problem 13:**

Write an equation of a vertical line through the point (-2, 6).

## Problem 14:

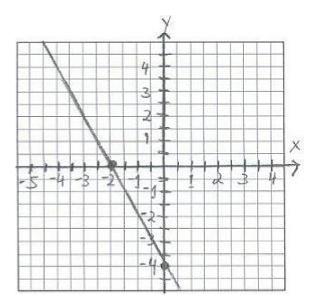
Write an equation of a line with undefined slope through the point (3, -5).

# **Problem 15:**

Write an equation of a horizontal line through the point (-2, 6).

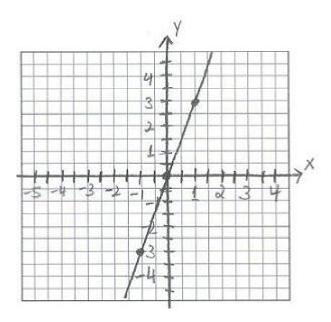
## **Problem 16:**

Find the general equation of the following line.



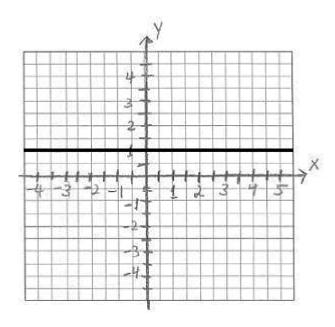
# **Problem 17:**

Find the slope intercept equation of the following line.



# **Problem 18:**

Find the slope-intercept equation of the following line.



## Problem 19:

Are the lines y = -x + 3 and y = 5 - x parallel? Answer Yes or No!

# Problem 20:

Are the lines y = -x + 3 and y - x = 2 parallel? Answer Yes or No!

## Problem 21:

Are the lines  $\mathbf{y} = -\frac{2}{3}\mathbf{x} + \mathbf{3}$  and  $\mathbf{y} = \frac{3}{2}\mathbf{x} + \mathbf{6}$  perpendicular? Answer Yes or No!

# Problem 22:

What is the slope of a line perpendicular to the line y = 2x - 5?

# Problem 23:

Write the Slope-Intercept Equation of a line through point (2, 5). The new line is to be parallel to the line 9x - 3y = -6.

## Problem 24:

Find the *Slope-Intercept Equation* of a line through point (-1, 3). The new line is to be perpendicular to the line x - 3y = 12.

# **SOLUTIONS**

You can find detailed solutions below the link for this problem set!

1. $4x + 3y = 8$	2. x - 2y = 7	3. a. $m = -1$ , $(0, 3)$ b. $m = \frac{4}{5}$ , $(0, -1)$ c. $m = 2$ , $(0, 0)$ d. $m = 1$ , $(0, 0)$ e. $m = 0$ , $(0, 1)$ f. $m = 0$ , $(0, -9)$ g. $m$ is undefined no y-intercept h. $m$ is undefined no y-intercept
4. m = 3, (0, 1)	5. $y = \frac{2}{3}x - 2$	6. $y = -12x + 20$
7. $y = 2x + 3$	8. a. $y = 2x - 5$ b. $y = -5x$ c. $y = 3x + 1$ d. $y = -7$	9. y = -x + 3
10. x = 1	11. y = 1	12. $2x + 3y = -9$
13. x = -2	14. x = 3	15. y = 6
16. $2x + y = -4$	17. $y = 3x$	18. y = 1
19. Yes	20. No	21. Yes
$m_{perp} = -\frac{1}{2}$	23. y = 3x - 1	24. y = - 3x